

# The Joint Determination of TFP and Financial Sector Size

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- Introduction
- Contribution I
- Contribution II
- Model: General Environment
- Production Function
- Frictions in the credit market
- Bellman Equations
- Bargaining
- Equilibrium Conditions
  - Human Resource Constraint
  - No Arbitrage between professions
  - Threshold of Productivity
  - Capital Market Clearing
  - Output determination
- Equilibrium Characterization and Solution
- Capital Irrelevance
- Effects of frictions in the investment sector

## Summary (2/2)

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- The degree of product market efficiency 
- Example 
- TFP and the size of the financial sector 
- Conclusions 
- A1 Effects of the destruction rate 
- A2 Effects of the bargaining power 



- Misallocation of resources to explain TFP differences across countries.
  - Extensive Margin (too many firms)
  - Intensive Margin (bad firms using too many resources)
  - Hopenhayn..., HsiehKlenow09, RestucciaRogerson08, etc.



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- modeling non-Walrasian features of investment markets
  - **Search Frictions**
    - WasmerWeil04, SilveraWright10, WangBesciLi05, denHaanetal03, Dell'AricciaGariba
    - Information frictions, time usage, creditor-borrower relationships...
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  - **Resources in intermediation**
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- We build a model of **Misallocation**
  - **Endogenizing** the degree of imperfections in **Capital Markets**
  - via **Search frictions**

- We impose aggregate resource constraints on
  - Capital, and
  - Human Resources
    - for financial intermediation
    - or directly productive activities



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- **Irrelevance of Capital Abundance.** For resource (mis)allocation

## Contribution II

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- Credit Market Frictions



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- Credit Market Frictions  $\Rightarrow$  Lower firm productivity



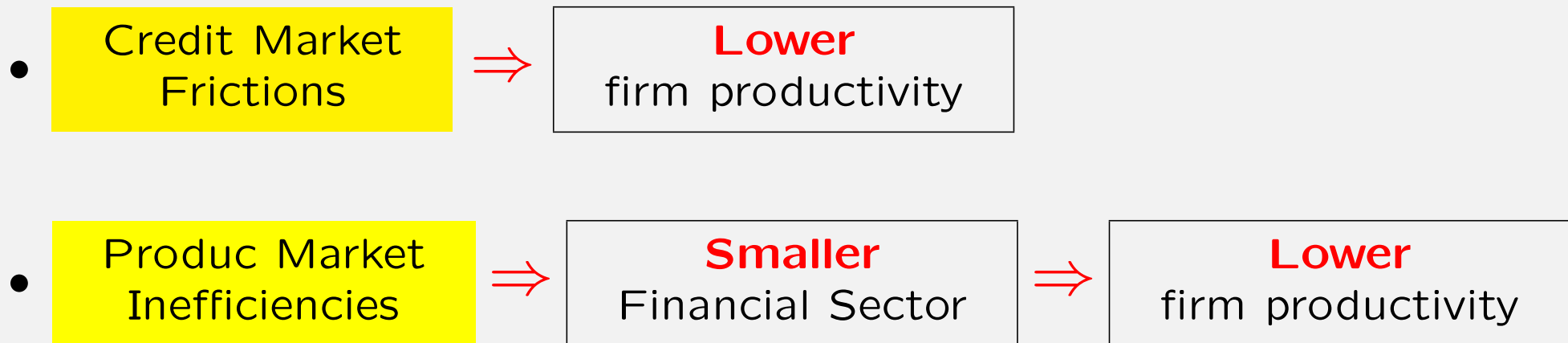
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- Product Market Inefficiencies

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- To explain cross countries differences in Productivities and GDP (TFP):
  - Underlying differences in **Product Market Efficiency**

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- Product Market Inefficiencies  $\Rightarrow$  Smaller Financial Sector  $\Rightarrow$  Lower firm productivity
- To explain cross countries differences in Productivities and GDP (TFP):
  - Underlying differences in **Product Market Efficiency**
- Rich countries are rich **and have a larger financial sector** because they have more efficient **product markets**
  - Not because more efficient financial sector.

## Two Markets (rooms):



- **Deposit Market:**
  - Walrasian.
  - market return  $r$ .
  - Inelastic supply  $\bar{k}$
- **Investment Market:**
  - time to find finance.
  - **Search frictions**
  - **heterogeneous projects**
  - specific evaluators
    - $\sim$  different beliefs

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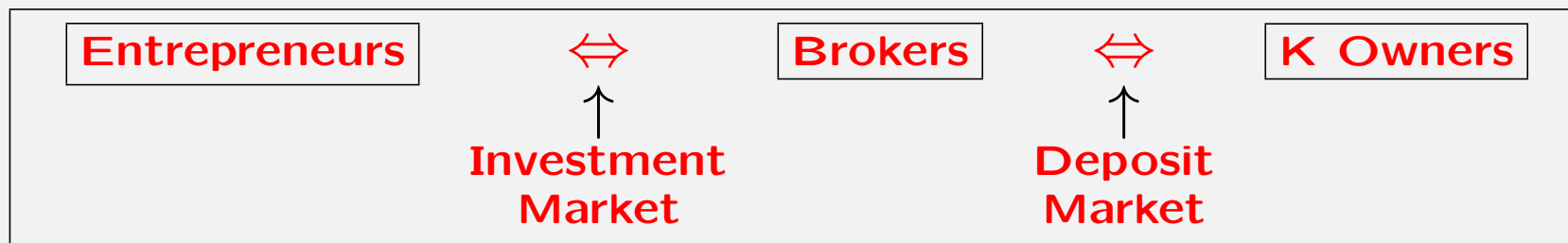
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- Project produces flow of income  $F(k; a, Y)$ 
  - $F_k(k; a, Y) > 0$ ,  $F_a(k; a, Y) > 0$ ,  $F_{ka}(k; a, Y) > 0$ ,  $F_{kk}(k; a, Y) < 0$
  - $Y$  measure of aggregate demand or market size.
    - We may well have  $F_Y = 0$  (neoclassical)
- Each unit of capital gets rent  $r$
- Profit generated by a project
  - $\pi(a, r, Y) = \max_k \{F(k, a, Y) - rk\}$ ,
  - Capital demand  $k^d(a, r)$ .
- $F(k, a, Y)$  is log linear in  $k$ ,  $a$ , and  $Y$

$$\pi(a, r, Y) = (1 - e_k) e_k^{\frac{e_k}{1-e_k}} a^{\frac{e_a}{1-e_k}} r^{-\frac{e_k}{1-e_k}} Y^{\frac{e_y}{1-e_k}}$$
$$\frac{rk^d(a, r, Y)}{\pi(a, r, Y)} = \frac{e_k}{1 - e_k}$$

- $e_k$ ,  $e_a$  and  $e_y$  are the (constant) elasticities.

- Brokers ease frictions in the market
  - the more there are,
    - the less time it takes for a manager to obtain funding.
  - Resource constraint:
    - If they are brokers, they are not entrepreneurs.
- A broker may have relationships with many entrep.
  - Once she meets an entrep. move on to look for another.
- Tightness:  $\theta = \frac{\text{mass of searching entrepreneurs}}{\text{mass of brokers}}$
- Rate at which entrep. meet brokers:  $p(\theta, \nu)$ ,  $\frac{\partial p(\theta, \nu)}{\partial \theta} < 0$ 
  - e.g., with  $\nu$  an exog. efficiency parameter  $p(\theta, \nu) = \nu\theta^{-\alpha}$
- CRS matching: for brokers  $\theta p(\theta, \nu)$
- Jointly learn productivity ( $a$ )
  - Threshold productivity  $b$



- Death rate  $\delta$  equals discount (and replacement)
- Entrepreneurs. Two states:

$$\begin{aligned}\delta V_0 &= p(\theta) \int_b^\infty [V_1(a) - V_0] dG(a) \\ \delta V_1(a, r, Y) &= \pi(a, r, Y) - \rho(a, r, Y)\end{aligned}$$

- $\rho(a, r) \equiv$  annuity of the payment to broker.
- continuation value of being a broker ( $B$ ) solves:

$$\delta B = \theta p(\theta) \int_b^\infty \Gamma(a) dG(a),$$

with  $\Gamma(a) = \frac{\rho(a, r, Y)}{\delta}$ .

- If  $a > b$ : **Bilateral Monopoly**. Nash bargaining
  - entreps.' bargaining weight  $\beta \in (0, 1)$

$$\begin{aligned}\beta S(a) &= V_1(a) - V_0 \\ (1 - \beta) S(a) &= \Gamma(a)\end{aligned}$$

- **Outside options**
  - Broker: **zero**
    - No satiation
    - Looks for new customer indep. of bargaining result.
  - Entrepreneur: **Get new project**
    - can NOT use the info acquired from broker.
    - Bargain on “schedule” ex-ante.
- This gives payment:  $\rho(a, r, Y) = (1 - \beta) \{ \pi(a, r, Y) - \delta V_0 \}$
- Broker accesses deposit market & extracts capital for project.
  - The **efficient** capital demand.

- $V_0 \equiv$  PDV of future income.

$$\delta V_0 = \frac{p(\theta) [1 - G(b)]}{\delta + p(\theta) [1 - G(b)]} \times \frac{\frac{\beta}{1-\beta}}{\frac{\beta}{1-\beta} + \frac{\delta}{\delta + p(\theta) [1 - G(b)]}} \times \int_b^\infty \pi(a, r, Y) \frac{dG(b)}{1 - G(b)} \quad (1)$$

- $\left( \frac{\delta}{\delta + p(\theta) [1 - G(b)]} \right)$  percentage of time searching
- $\left( \int_b^\infty \pi(a, r, Y) \frac{dG(b)}{1 - G(b)} \right)$  expected income flow of project with  $a > b$ .
- $\left( \frac{\frac{\beta}{1-\beta}}{\frac{\beta}{1-\beta} + \frac{\delta}{\delta + p(\theta) [1 - G(b)]}} \right)$  share of this income for entrepreneur.
- The value of a broker:

$$\delta B = \frac{\theta p(\theta) [1 - G(b)]}{\delta + \theta p(\theta) [1 - G(b)]} \frac{\frac{1-\beta}{\beta}}{\frac{1-\beta}{\beta} + \frac{\delta}{\delta + \theta p(\theta) [1 - G(b)]}} \times \int_b^\infty \pi(a, r, Y) \frac{dG(b)}{1 - G(b)}$$

- $m \equiv$  number of entrepreneurs.
- endogenous variables:  $\{\theta, m, r, b, Y\}$ .
- The equilibrium conditions:
  - **Human Resource Constraint:**  $\theta = \frac{\text{searching entrep}}{1-m}$
  - **No Arbitrage between professions:**  $V_0 = B$
  - **Threshold of Productivity:**  $b : S(b) = 0$
  - **Capital Market Clearing:**  $K^d(r, b, m) = \bar{k}$
  - **Output determination** Aggregate demand equals output.

- $\theta = \frac{\delta}{\delta + p(\theta)[1 - G(b)]} \frac{m}{1 - m}$ . Substituting:

$$1 - m = \frac{\delta}{\theta [\delta + p(\theta, \nu) (1 - G(b))] + \delta}$$

- more human resources devoted to financial activities  $\Rightarrow$  larger  $b$ .
- Given  $\theta$ , if  $b$  increases, the number of rejections also increases,
  - the share of *searching* entrepreneurs also increases,
  - increase in size of the financial sector to keep  $\theta$  constant.
- Larger financial sector allows society to be pickier in quality of projects

Finance does not produce output directly,

- Allows to improve productivity of firms
- by reducing the opportunity cost of searching for better projects.

# No Arbitrage between professions



No arbitrage between professions pins down credit market tightness

$$V_0 = B \Rightarrow \theta = \frac{\beta}{(1-\beta)}$$

- $\theta$  depends only on the bargaining power. Independent of  $b$
- Entrepreneur and broker care only about **expected** incomes.
  - Time searching compensates for **share** of the deal
  - Independently of **size** of the deal
- More ( $\beta$ ), better for entrep.
  - Longer search to equalize value across activities.
- 2 ways of decreasing  $\theta$  (ratio searching entrepreneurs to brokers).
  - Increasing the number of brokers (more finance/GDP)
  - Increasing the threshold of productivity
    - Smaller numerator via more rejections.

- $b$  :  $S(b) = 0 \Leftrightarrow \delta V_1(b) = \delta V_0$ 
  - because continuation value of broker independent of events in match

$$\delta V_1(a) = \delta V_0 + \beta [\pi(a, r, Y) - \delta V_0]$$

- projects accepted if profits that they generate are larger than the value of going back into search.

- $b$  is such that  $\pi(b, r, Y) = \delta V_0$

$$\frac{\pi(b, r, Y)}{\int_b^\infty \pi(a, r, Y) \frac{dG(b)}{1-G(b)}} = \frac{p(\theta) [1 - G(b)]}{\delta + p(\theta) [1 - G(b)]} \times \frac{\frac{\beta}{1-\beta}}{\frac{\beta}{1-\beta} + \frac{\delta}{\delta + p(\theta) [1 - G(b)]}}$$

- $$\frac{\pi(b, r, Y)}{\int_b^\infty \pi(a, r, Y) \frac{dG(b)}{1-G(b)}} = \frac{p(\theta)[1-G(b)]}{\delta + p(\theta)[1-G(b)]} \times \frac{\frac{\beta}{1-\beta}}{\frac{\beta}{1-\beta} + \frac{\delta}{\delta + p(\theta)[1-G(b)]}}$$

- RHS: PDV of the share of the income that goes to the entrepreneurs.
    - decreasing in  $b$ , and equals zero as it approaches its upper limit.

- LHS: **ratio of marginal to average profits.**

$$H(b, \epsilon) \equiv \frac{\pi(b, r, Y)}{\int_b^\infty \pi(a, r, Y) \frac{dG(a)}{1-G(b)}} = \frac{(b)^\epsilon}{\int_b^\infty (a)^\epsilon \frac{dG(a)}{1-G(b)}} \in (0, 1)$$

where  $\epsilon$  is the elasticity of profits to  $a$ :  $\epsilon = \frac{e_a}{1-e_k}$

- Intuitive  $H(b, \epsilon)$  to be non-decreasing in  $b$ . Thus, assumption on  $G(\cdot)$ 
  - $H$  is a non-decreasing function of  $b$ :  $\frac{\partial H(b, \epsilon)}{\partial b} \geq 0$
  - Includes many (if not all) of the commonly used distributions.



- $K^d(r, b, m) = \bar{k}$ .

$$\frac{p(\theta) [1 - G(b)]}{\delta + p(\theta) [1 - G(b)]} m \int_b^\infty k^d(a, r) \frac{dG(a)}{1 - G(b)} = \bar{k}$$

$$\frac{p(\theta) [1 - G(b)]}{\delta + p(\theta) [1 - G(b)]} m \int_b^\infty \frac{e_k}{1 - e_k} \pi(a, r, Y) \frac{dG(a)}{1 - G(b)} = r \bar{k} \quad (2)$$

- average lifetime income equals the annuity of the profit of the marginal firm:  $\delta V_0 = \pi(b, r)$

$$\delta V_0 = \frac{\beta p(\theta)[1 - G(b)]}{\delta + \beta p(\theta)[1 - G(b)]} \int_b^\infty \pi(a, r) \frac{dG(a)}{1 - G(b)} \quad (3)$$

$$Y = r\bar{k} + \frac{1}{\delta} \pi(b, r, Y) \quad (4)$$

The solution algorithm:

- Arbitrage pins down  $\theta$ .
- Optimal Threshold pins  $b$
- $1 - m$  is obtained from the human resource constraint
- $r$  and  $Y$  are residuals

**Result:** *The threshold of productivity  $b$  is the unique solution of:*

$$\frac{(b)^\epsilon}{\int_b^\infty (a)^\epsilon \frac{dG(a)}{1-G(b)}} = \frac{p(\theta, \nu) [1 - G(b)]}{\delta + p(\theta, \nu) [1 - G(b)]} \times \frac{\frac{\beta}{1-\beta}}{\frac{\beta}{1-\beta} + \frac{\delta}{\delta + p(\theta, \nu) [1 - G(b)]}} \quad (5)$$

**Result:** *Given the value of  $b$  determined in result . The number of brokers in the economy (and the share of finance in GDP) is:*

$$1 - m = (1 - \beta) (1 - H(b, \epsilon)) \quad (6)$$

**Result:** *Given  $b$  from result*

$$r\bar{k} = \frac{e_k}{1 - e_k} \pi(b, r, Y) \quad (7)$$

$$Y = \left[ \frac{e_k}{1 - e_k} + \frac{1}{\delta} \right] \pi(b, r, Y)$$

*Furthermore, both  $r$  and  $Y$  are maximized whenever  $b$  is maximum*

**Result:** *The allocative decisions of the economy  $\theta$ ,  $m$  and  $b$  are independent of  $\bar{k}$ .*

- To have more or less  $K$  (and thus  $r$ ) does not affect the marginal to average profit ratio ( $H(b, \epsilon)$ ),
- correlation across countries of income and financial sector size
  - can not be simply because relative capital abundance.

**Result:**  *$b$  and output are both increasing in the efficiency of the search process in the investment sector ( $\nu$ ). Furthermore, as  $\nu$  approaches infinity the limit of  $b$  is its maximum possible value (or infinity if it is unbounded).*

*The number of brokers,  $(1 - m)$  is decreasing with  $\nu$ .*

- Less frictions, More picky
  - smaller opportunity cost of back to search.
- Less frictions, Less brokers
  - They are not needed. Few get many matches.
- Walrasian Limit:  $b = \bar{a}$ ,  $m = 1$

**Result:** *The minimum productivity threshold  $b$  (and consequently  $Y$ ) are increasing in the elasticity of profits to talent ( $\epsilon$ ), irrespectively of the shape of  $H(b, \epsilon)$ .*

*The number of brokers increases with  $\epsilon$ .*

- Productivity more important.
  - You are more picky about the quality of the projects you start.
  - More option value of looking for a better project.
- More picky. More projects rejected.
- More *searching* entrepreneurs
- More Brokers to service them ( $\theta$  constant)

- Consider tax and transfer scheme (Benabou, 2002). The net profits of a firm are:

$$\hat{\pi}(a, r) = \pi(a, r)^{1-\tau} \tilde{\pi}^{\tau}$$

- $\tau$  : measures progressive redistribution between efficient and non-efficient firms
  - $\tilde{\pi}$  is perceived by the agents as lump-sum
- Clearly, balanced budget requires:

$$\int_b^{\infty} \pi(a, r) \frac{dG(a)}{1 - G(b)} = \int_b^{\infty} \hat{\pi}(a, r) \frac{dG(a)}{1 - G(b)}$$

- In our environment  $\tau$  measures allocative inefficiencies in the economy.
  - Higher  $\tau$  transfers profitability from efficient to inefficient firms



- $\tau$  decreases elasticity of profits to productivity:

$$H(b, \epsilon, \tau) = \frac{\hat{\pi}(b, r)}{\int_b^\infty \hat{\pi}(a, r) \frac{dG(a)}{1-G(b)}} = \frac{(b)^{\epsilon(1-\tau)}}{\int_b^\infty a^{\epsilon(1-\tau)} \frac{dG(a)}{1-G(b)}}$$

**Result:** *A decrease of the allocative inefficiencies of the product sector (decrease of  $\tau$ ) produces larger steady state values of  $b$  and  $Y$  and a decrease of  $m$*

- More efficient treatment of firms. More Picky
- ... and more brokers.

## Example (1/4)



- $F(a, K, Y) = 2\sqrt{aK}$
- $1 - \tau$  measures the efficiency of the productive sector.
- $a$  follows a Pareto with minimum value  $\underline{a}$  and parameter  $\gamma$

$$\pi(a, r) = \frac{a}{r}; \quad k^d(a, r) = \frac{a}{r^2}; \quad \hat{\pi}(a, r) = \left(\frac{a}{r}\right)^{1-\tau} \tilde{\pi}^\tau; \quad \tilde{\pi} = \left(\frac{\gamma - (1 - \tau)}{\gamma - 1}\right)^{\frac{1}{\tau}} b$$

$$\left( H(b, 1 - \tau) = \frac{\gamma - (1 - \tau)}{\gamma} \right)$$

**Result:**

There exists a level of taxes  $\tilde{\tau} = \frac{1 - (\gamma - 1) \frac{1}{\beta} \frac{\delta}{p\left(\frac{\beta}{1-\beta}, \nu\right)}}{1 + \frac{1}{\beta} \frac{\delta}{p\left(\frac{\beta}{1-\beta}, \nu\right)}} \in (0, 1)$  such that

$$\begin{aligned}
 1 - G(b) &= \begin{cases} 1 + \frac{1}{\beta} \frac{\delta}{p\left(\frac{\beta}{1-\beta}, \nu\right)} \frac{\tau + \gamma - 1}{1 - \tau} & \text{if } \tau \leq \tilde{\tau} \\ 1 & \text{if } \tilde{\tau} \leq \tau \end{cases} \\
 b &= \begin{cases} \underline{a} \left[ \beta \frac{p\left(\frac{\beta}{1-\beta}, \nu\right)}{\delta} \frac{1 - \tau}{\tau + \gamma - 1} \right]^{\frac{1}{\gamma}} & \text{if } \tau \leq \tilde{\tau} \\ \underline{a} & \text{if } \tilde{\tau} \leq \tau \end{cases} \\
 1 - m &= \begin{cases} (1 - \beta) \frac{1 - \tau}{\gamma} & \text{if } \tau \leq \tilde{\tau} \\ (1 - \beta) \frac{1}{1 + \beta \frac{p\left(\frac{\beta}{1-\beta}, \nu\right)}{\delta}} & \text{if } \tilde{\tau} \leq \tau \end{cases}
 \end{aligned} \tag{8}$$

## Example (3/4)



From where TFP,  $r$  and income:

$$A = \begin{cases} b \left(1 + \frac{\tau}{\gamma-1}\right) = \underline{a} \left[ \beta \frac{p\left(\frac{\beta}{1-\beta}, \nu\right)}{\delta} \frac{1-\tau}{\tau+\gamma-1} \right]^{\frac{1}{\gamma}} \left(1 + \frac{\tau}{\gamma-1}\right) & \text{if } \tau \leq \tilde{\tau} \\ \underline{a} \frac{\gamma}{\gamma-1} \frac{\beta \frac{p\left(\frac{\beta}{1-\beta}, \nu\right)}{\delta}}{1 + \beta \frac{p\left(\frac{\beta}{1-\beta}, \nu\right)}{\delta}} & \text{if } \tilde{\tau} \leq \tau \end{cases}$$

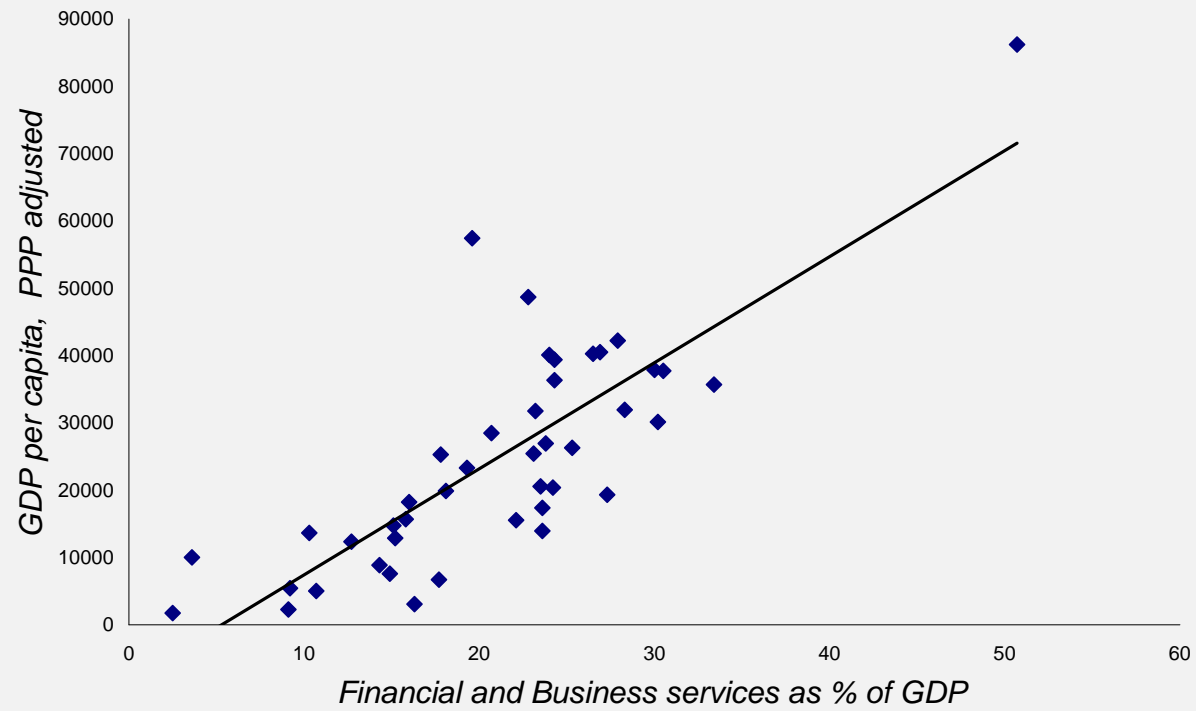
$$r = \frac{\sqrt{A}}{\sqrt{k}}$$

$$Y = 2\sqrt{A}\sqrt{k}$$

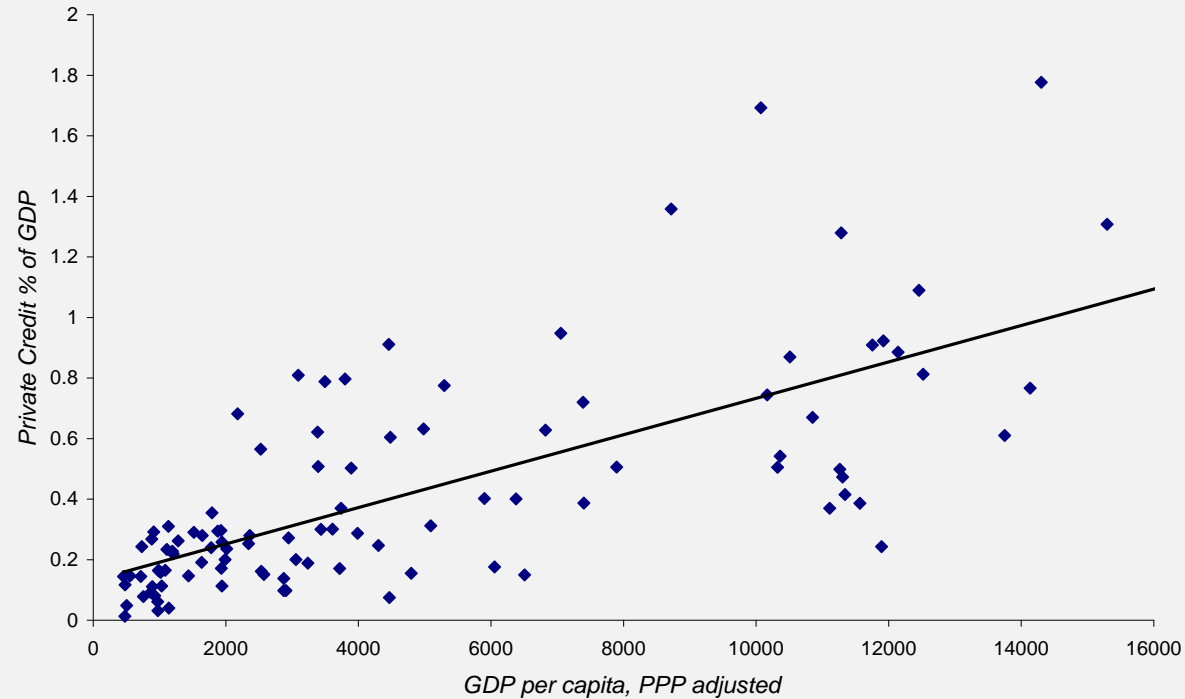
$$A = \begin{cases} b \left(1 + \frac{\tau}{\gamma-1}\right) = \underline{a} \left[ \beta^p \frac{\left(\frac{\beta}{1-\beta}, \nu\right)}{\delta} \frac{1-\tau}{\tau+\gamma-1} \right]^{\frac{1}{\gamma}} \left(1 + \frac{\tau}{\gamma-1}\right) & \text{if } \tau \leq \tilde{\tau} \\ \underline{a} \frac{\gamma}{\gamma-1} \frac{\beta^p \left(\frac{\beta}{1-\beta}, \nu\right)}{1 + \beta^p \frac{\left(\frac{\beta}{1-\beta}, \nu\right)}{\delta}} & \text{if } \tilde{\tau} \leq \tau \end{cases}$$

- Less frictions in finance,  $\uparrow \nu \rightarrow \uparrow A$  via two different mechanisms.
  - More efficient firms ( $\uparrow b$ ),
  - but also makes them smaller ( $\uparrow m$ )  $\rightarrow \uparrow$  productivity of capital.
- More efficient product sector ( $\downarrow \tau$ ): effects in opposite directions.
  - $\uparrow b \Rightarrow \uparrow A$  via selection.
  - But,  $\downarrow m \Rightarrow$  Larger firms  $\Rightarrow$  More capital per firm  $\Rightarrow \downarrow A$
  - First effect dominates, **always**.

- Cross country evidence: Positive correlation  $(1 - m)$  with  $A$ .
- Traditional Explanation: Schumpeterian, King and Levine (1993)
  - Better finance, more growth

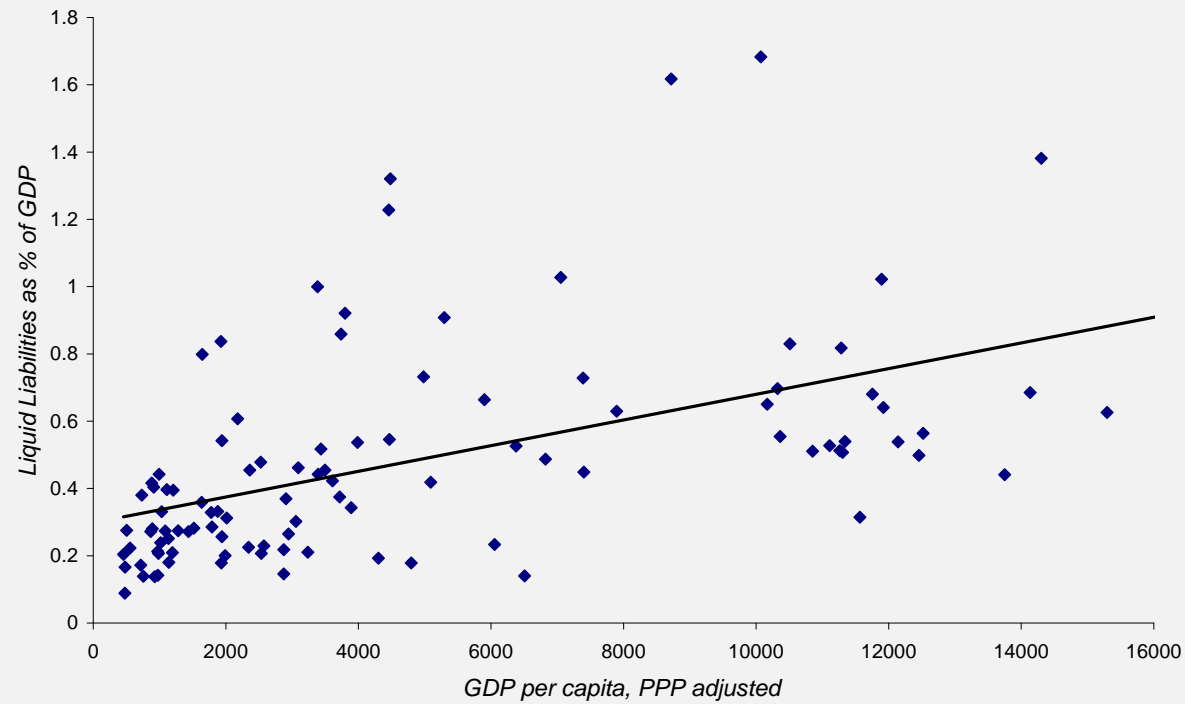


[Financial and Business Services as % of GDP.]

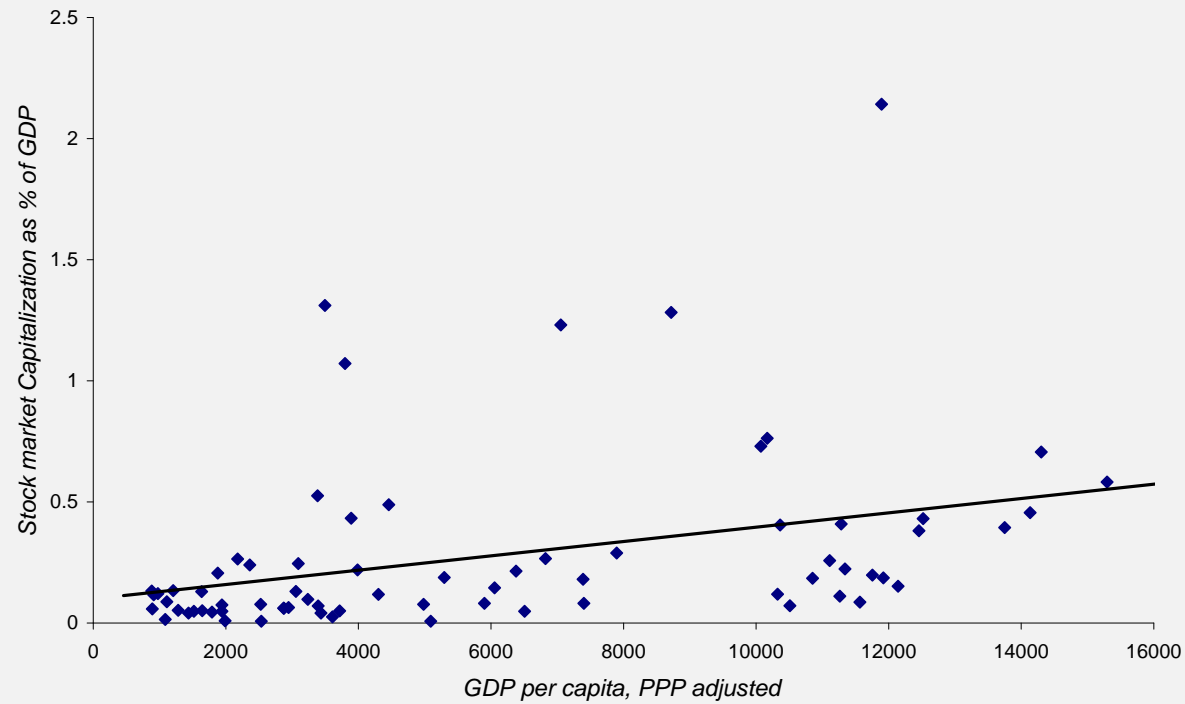


[Claims on private sector by deposit money banks and other financial institutions as % of GDP]

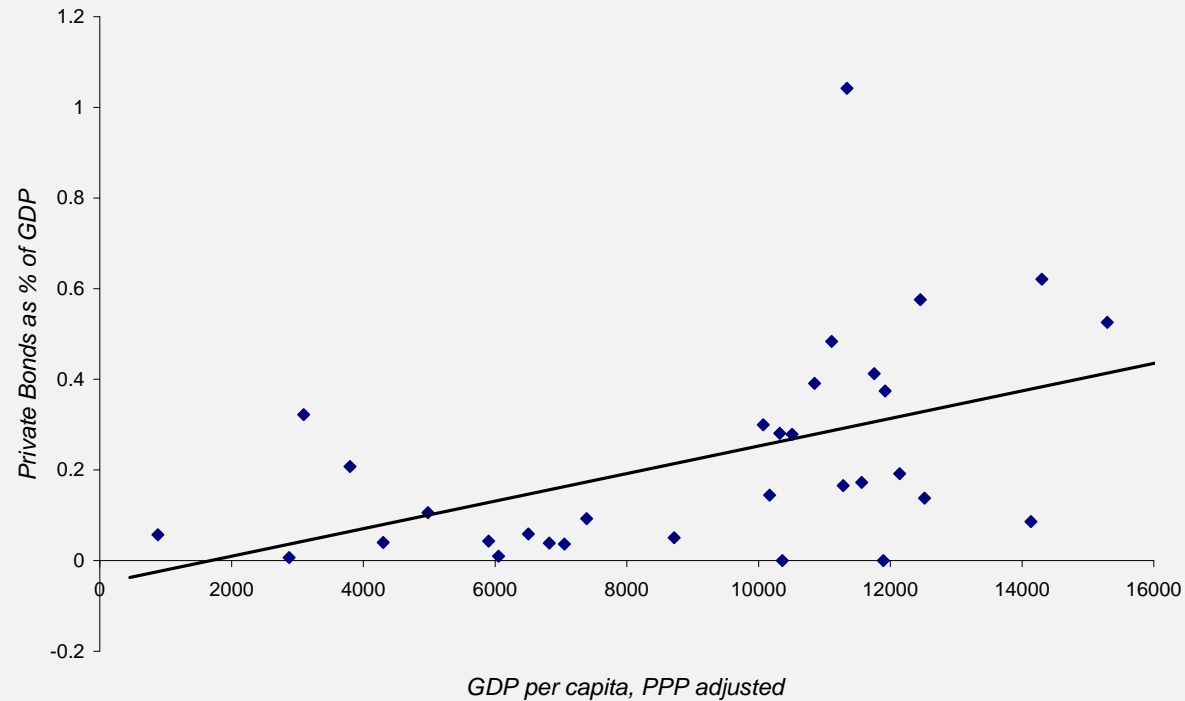




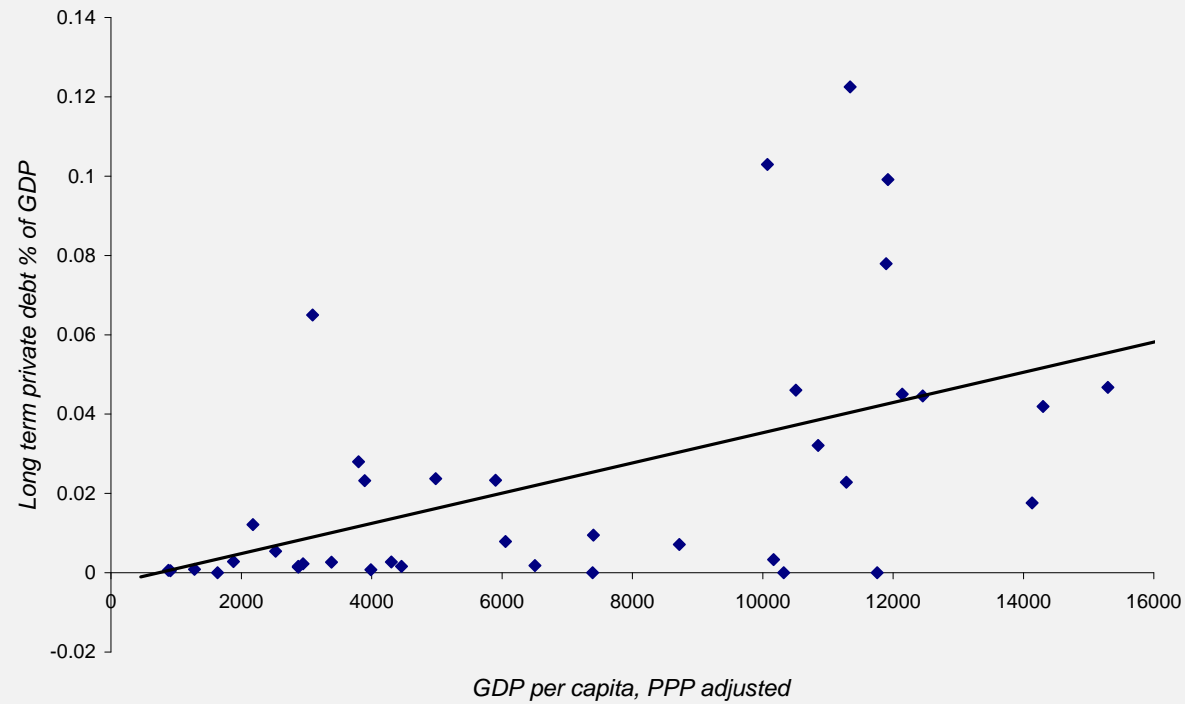
[Liquid liabilities as % of GDP]



[Stock Market capitalization as % of GDP ]



[Outstanding domestic debt securities issued by private domestic entities divided by GDP]



[Total private long-term debt issues as % of GDP]



- The level of capital does not seem to affect the relationship
- Neusser and Kugler (1998)
  - Finance size cointegrated with TFP in manufacturing
    - not with output
  - They find evidence of reverse causality.
- In our model:
  - Differences in  $\nu$  would produce **negative** correlation.
  - Differences  $\tau$  would produce positive correlation.
  - Contractual inefficiencies ( $\beta$ ) can explain both only if they mean that there is too little power to brokers, and not in Pareto-World

**Result:** *Model suggest that the rich countries are rich and have a larger financial sector because their product sectors have more allocative efficiency, not because they have a more efficient financial sector.*

- Tractable model.
  - Capital Irrelevant.
- Less frictions in financial markets
  - More income
  - Less dispersion of firm characteristics
  - LESS financial sector
- More destruction (here not creative, but perhaps...)
  - Less income.
  - More dispersion
  - More financial sector.
- There can be Too much or too little contractual power into finance.
- Efficiency in Product Market delivers
  - More income
  - Less dispersion
  - More finance
- Compatible with data if differences across countries are derived mostly from inefficiencies in product markets, not in financial markets.

# A1 Effects of the destruction rate



**Result:**  $b$  is not increasing in  $\delta$ , and strictly **decreasing** if  $H(b, \epsilon)$  is strictly increasing in  $b$ .

*The number of entrepreneurs does not decrease with  $\delta$ , and strictly **increase** if  $H(b, \epsilon)$  is strictly increasing in  $b$ .*

- Less time before death ( $\uparrow \delta$ ). Less picky
- but increase in brokers... because many newborns.
- Large destruction rate demands large finance sector.



**Result:** *There exists a value of  $\beta$  called  $\hat{\beta} : 1 - \hat{\beta} = -\frac{\theta}{p(\theta, \nu)} \frac{\partial p(\theta, \nu)}{\partial \theta}$  such that  $\hat{\beta}$  maximizes  $b$  (and thus,  $Y$ ). If  $\beta < \hat{\beta} \rightarrow \frac{db}{d\beta} > 0$ , and if  $\beta > \hat{\beta} \rightarrow \frac{db}{d\beta} < 0$ .*

*An increase of  $\beta$  decreases  $1 - m$  if  $\beta < \hat{\beta}$ . If the value of  $\beta$  is much larger than  $\hat{\beta}$ , it is possible than an increase of  $\beta$  might increase  $1 - m$*

- $\beta$ , contractual arrangements...
- $\beta$  has two effects:
  - More “share” to entrep.
  - but increases her waiting time.
    - Get later
    - and less (outside option)
- like HOSIOS... it IS Hosios.
  - Congestion in search pool, interiorized if  $\beta = \hat{\beta}$

# The Joint Determination of TFP and Financial Sector Size

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